Substitution method

$$a_1x + b_1y + c_1 = 0$$
 ...(i)
 $a_2x + b_2y + c_2 = 0$...(ii)

From eq. (i)
$$x = \frac{-c_1 - b_1 y}{a_1}$$

Substitute x in eq. (ii) and solve.

$$x = \frac{b_1 c_2 - b_2 c_1}{a_1 b_2 - a_2 b_1}$$

$$y = \frac{a_2c_1 - a_1c_2}{a_1b_2 - a_2b_1}$$

Elimination method

$$a_1x + b_1y + c_1 = 0$$
 ...(i)
 $a_2x + b_2y + c_2 = 0$...(ii)

Multiply bz in (i) & bt in (ii)

$$a_1b_2x + b_1b_2y + c_1b_2 = 0$$
 ...(iii)

$$b_1 a_2 x + b_2 b_1 y + c_2 b_1 = 0$$
 ...(iv)

(3) -(4)

$$(a_1b_2-b_1a_2)x + (c_1b_2-c_2b_1) = 0$$

$$x = \frac{b_1 c_2 - b_2 c_1}{a_1 b_2 - a_2 b_1}$$

$$y = \frac{a_2c_1 - a_1c_2}{a_1b_2 - a_2b_1}$$

e.g. Six years hence a man's age will be three times the age of his son and three years ago he was nine times as old as his son. Find their present ages.

Sol. Let man's present age be 'x' yrs & son's present age be 'y' yrs. According to problem

$$x + 6 = 3(y + 6)$$

$$x - 3y = 12...(i)$$

and
$$x - 3 = 9 (y - 3)$$

$$x - 9y = -24...$$
 (ii)

On solving equation (i) & (ii)

x = 30 and y = 6.

So, the present age of man = 30 years and present age of son = 6 years.

Linear equation

in two variables

$$a_1x + b_1y + c_1 = 0$$
 ...(1)
 $a_1x + b_2y + c_3 = 0$...(2)

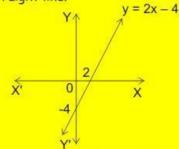
$$a_2x + b_2y + c_2 = 0$$
 ...(2)

Methods to solve

Equation of a straight line

ax + by + c = 0 $\{a \neq 0, b \neq 0 \& a, b, c \in R\}$

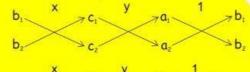
Solution $(x,y) \rightarrow point lying on$ straight line.



Algebraic method

Graphical method

Cross multiplication method



$$\frac{x}{b_1c_2 - b_2c_1} = \frac{y}{c_1a_2 - a_1c_2} = \frac{1}{a_1b_2 - a_2b_1}$$

$$x = \frac{b_1 c_2 - b_2 c_1}{a_1 b_2 - a_2 b_1}$$

$$y = \frac{a_2c_1 - a_1c_2}{a_1b_2 - a_2b_1}$$

Condition of Solvability of System of Linear Equations

Intersecting (intersect at 1 point)



Unique solution (consistent)

Coincident (Coincide)

 $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} \rightarrow \text{Infinite solution}$ (consistent)

Parallel (No intersection)

 $\xrightarrow{\text{tion}} \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \rightarrow \text{No solution}$ (inconsistent)

Equations reducible to a pair of linear equations

$$\frac{2}{x} + \frac{3}{y} = 13$$
, $\frac{5}{x} - \frac{4}{y} = -2$
Let

Let
$$\frac{1}{x} = p$$
, $\frac{1}{y} = q$ $2p + 3q = 13$ $5p - 4q = -2$

e.g. Solve the following system of linear equations graphically: x - y = 1, 2x + y = 8.

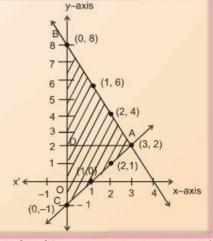
Sol.(i)
$$x - y = 1$$

 $x = y + 1$

(ii)

		- 2	1570	33
2x + y = 8 y = 8 - 2x	x	0	1	2
	v	8	6	4

Solution is x = 3 and y = 2



NCERT / X / Linear equation in two variable